## Diagnostic tests, Laboratory tests

. Introduction<br>॥. Informational values of a test<br>III. Consequences of the prevalence rate<br>iv. Sequential use of 2 tests<br>v. Selection of a threshold: the ROC curve<br>v. Laboratory tests

## I. Introduction

- Medical decision making:
- Relies on the observation of the reality
- This observation is not the realty, the observer must keep a critical mind
- Diagnostic test:
- Every information mean that is useful for medical decision making
- Binary response (0 or 1)
- Different kinds: interviewing, clinical exam, paraclinical exam (laboratory, imaging, etc.)
- Gold Standard
- Test that is considered to be exact
- Not always available of acceptable...


## I. Introduction

- Examples:
- Alzheimer's disease:
- Gold standard: post-mortem examination of the brain
- Usual test: clinical tests + brain imaging + laboratory
- Down Syndrome of the fetus:
- Gold standard: karyotype (dangerous and expensive)
- Usual test: triple test (lab) + echography
- Electrocardiogram interpretation
- Gold standard: senior cardiologist
- Test to evaluate: junior cardiologist, automated interpreter, etc.
- Reasons not to use the Gold Standard chronology, cost, risk, availability


## II. Informationnal value of a test

A. Terminology
B. Intrinsic validity
c. Extrinsic validity
D. Exercise

## Informational value of a test A. Terminology



$\mathrm{O}=$ observator<br>T=test R=realty

## Informational value of a test A. Terminology

# Blue set: Red set: 

With/without disease
Positive/negative test

D+/D-
T+/T-


$$
\begin{aligned}
& \mathrm{FN}=\mathrm{T}-\cap \mathrm{D}+ \\
& \mathrm{TP}=\mathrm{T}+\cap \mathrm{D}+ \\
& \mathrm{FP}=\mathrm{T}+\cap \mathrm{D}- \\
& \mathrm{TN}=\mathrm{T}-\cap \mathrm{D}-
\end{aligned}
$$

## Informational value of a test A. Terminology

|  | $\mathrm{D}_{+}$ | $\mathrm{D}-$ |
| :---: | :---: | :---: |
| $\mathrm{T}+$ | \# TP | \# FP |
| $\mathrm{T}-$ | \# FN | \# TN |

## Informational value of a test B. Intrinsic validity

## - Experimental conditions:

- We already know which patients are D+ or D-, we want to observe the result of the test
- "Pre-test probabilities"
- Sensitivity = Se

$$
\begin{aligned}
& =P(T+\mid D+) \\
& =T P /(T P+F N)
\end{aligned}
$$

- Specificity = Sp

$$
\begin{aligned}
& =\mathrm{P}(\mathrm{~T}-\mid \mathrm{D}-) \\
& =\mathrm{TN} /(\mathrm{TN}+\mathrm{FP})
\end{aligned}
$$

## Informational value of a test C. Extrinsic validity

- Practical use of the test:
- We can observe the result of the test (T+or T-) and we want to predict the status of the patients (D+ or D-)
- "Post-test probabilities"
- Positive predictive value = PPV

$$
\begin{aligned}
& =\mathrm{P}(\mathrm{D}+\mid \mathrm{T}+) \\
& =\mathrm{TP} /(\mathrm{TP}+\mathrm{FP})
\end{aligned}
$$

- Negative predictive value = NPV

$$
\begin{aligned}
& =\mathrm{P}(\mathrm{D}-\mid \mathrm{T}-) \\
& =\mathrm{TN} /(\mathrm{TN}+\mathrm{FN})
\end{aligned}
$$

## Exercise

- We interest on 150 patients from the Urology unit:
- test = PSA dosage (positive over 4ng/ml)
- disease = confirmed prostate cancer
- Compute the following numbers:
- Prevalence rate $P=$
- Se=
- $S p=$
- $\mathrm{PPV}=$
- NPV=



## III. Consequences of the prevalence rate of a disease

A. Bayes' Theorem
B. Intuitive presentation
c. Exercise
D. How to proceed for screening?

## Consequences of the prevalence rate A. Bayes' Theorem

- Let $P$ be the prevalence rate, $P=P(D+)$
- $\mathrm{PPV}=$
$\frac{S e^{*} P}{S e^{*} P+(1-S p)^{*}(1-P)}$
- NPV = $\frac{\mathrm{Sp}^{*}(1-\mathrm{P})}{\mathrm{Sp}^{*}(1-\mathrm{P})+(1-\mathrm{Se})^{*} \mathrm{P}}$


## Consequences of the prevalence rate B. Intuitive presentation



- Intrinsic validity: both Se \& Sp are computed using only one column, separately from the other
- Extrinsic validity: PPV \& NPV are computed using one line, including both columns
- The prevalence rate is in relation with the ratio between both columns
$=>$ modifies the extrinsic validity, not the intrinsic one


## Exercise

- In last exercise, we found:

$$
\begin{aligned}
\mathrm{P}= & 0.67 \\
-\mathrm{Se}= & 0.20 \\
\mathrm{Sp}= & 0.94 \\
-\mathrm{PPV}= & 0.87 \\
\mathrm{NPV}= & 0.37
\end{aligned}
$$

- Compute the PPV in both next populations:
- General population of men having age>74 years ( $\mathrm{P}=2.66 \%$ )
- General population of men having 45<age<55 years ( $P=0.06 \%$ )


## Consequences of the prevalence rate

 D. How to proceed for screening?- When a disease is rare (all the diseases are rare!):
- Intrinsic validity is not affected ...but useless for medical decision making
- Increase of the NPV A negative test is comforting
- Strong decrease of the PPV Strong risk to wrongly announce a diagnosis!
- How to proceed:
- Only use the test only in a very meaningful context (increased prevalence rate): compatible clinical picture, exposure to an infectious disease, risk factor, etc.
- Only few tests can be used for mass screening. Most often, they are coupled with confirmation tests (with higher PPV)


## IV. Sequential use of 2 tests

## $1^{\text {st }}$ test : screening

[-] negative $\quad[+]$ positive

## Negative

Example of screening schema:

- Use a $1^{\text {st }}$ test with high sensitivity and then excellent NPV, because in addition the disease is rare
- Confirm with a $2^{\text {nd }}$ test having a high PPV
notably because the population has been selected before!
!!! Ideally, the misclassification of both tests is not due to the same factors, T1 and T2 are of different natures (e.g. lab \& imaging)
- The result is positive if and only if both tests are positive


## Exercise

## $\mathrm{T}_{1}$ :

PSA dosage
[-] negative $\quad[+]$ positive
( $<4 \mathrm{ng} / \mathrm{ml}$ ) ( $>4 \mathrm{ng} / \mathrm{ml}$ )
$\mathrm{T}_{2}$ :
imaging
[-] negative [+] positive

## Negative

- We study 100,000 people from the general population having age>80 ( $\mathrm{P}=2.66 \%$ ).
- T+ = $\mathrm{T}_{1}+\cap \mathrm{T}_{2}+$
- $\mathrm{T}_{1}$ : $\mathrm{Se}=0.2 \& \mathrm{Sp}=0.94$
- $\mathrm{T}_{2}$ : $\mathrm{Se}=0.5 \& \mathrm{Sp}=0.95$
- What is the PPV of T? use
$P P V=\frac{S^{*}{ }^{\star} \mathrm{P}}{\mathrm{Se}^{\star} \mathrm{P}+(1-\mathrm{Sp})^{\star}(1-\mathrm{P})}$


## V. Selection of a threshold: the ROC curve

A. Introduction
B. Construction
c. Interpretation
D. Selection of the best threshold
E. Exercise

## Selection of a threshold: ROC curve A. Introduction

## $O \rightarrow T \xrightarrow[\substack{T h_{3}}]{\substack{T h_{1}}} \underset{\substack{T h_{1}}}{\longrightarrow} R$ <br> O=observator T=test <br> Th=threshold <br> $\mathrm{R}=$ realty

## Problem:

- A test provides with a quantitative response
- We wish to binarize the output (yes/no)
- Depending on the chosen threshold, the prediction differs...


## Selection of a threshold: ROC curve B. Construction

## $Y=S e$



- ROC curve: simply displays the $\{\mathrm{Se} ; \mathrm{Sp}\}$ couples that are found using different thresholds
- Abscissa : X=1-Sp
- Ordinate : Y=Se


## Selection of a threshold: ROC curve C. Interpretation



- AUC=Area

Under the Curve

- $0.5 \leq A U C \leq 1$

- Perfect point with $\mathrm{Se}=\mathrm{Sp}=1$
- $A U C=1$

- "hasard diagonal" (useless test)
- $A U C=0.5$


## Selection of a threshold: ROC curve D. Selection of the best threshold

$Y=S e$


- Selection of the best threshold: point that is closer to the perfect point
- Minimizing the [a;b] distance means minimizing $(1-\mathrm{Se})^{2}+(1-\mathrm{Sp})^{2}$


## Exercise

- As in exercise 1, we compute Se and Sp using several thresholds for the PSA dosage.
- We get the present table:

| Threshold | Se | Sp |
| :---: | :---: | :---: |
| 1 | 0.83 | 0.39 |
| 2 | 0.52 | 0.72 |
| 4 | 0.20 | 0.94 |

- Trace the ROC curve.
- Which threshold would you choose using the geometric criterion?


## Exercise

- We analyze the ability of the Glasgow University Interpreter to automatically detect "atrial fibrillation" by analyzing ECGs from a database.
- We find the following (there are 2 thresholds in the software):
- $\mathrm{Se}=0.923$
- $\mathrm{Se}=0.923 \quad \mathrm{Sp}=0.987$

$$
\mathrm{PPV}=0.462 \quad \mathrm{NPV}=0.999
$$

- Roc curve: AUC=0.96
- What do you think about it? Can it be used to replace the Cardiologists? Why is the PPV quite low?


## VI. Laboratory tests

## I. Distributions

I. Interval of normal values, alpha and beta risks
III. Effect of the population on the normal values
iv. Multiple testing

## Biological parameters

- Dosages from various liquids or tissues (blood, urine, cerebrospinal fluid...)
- We interest on exams that output a quantitative response (most of them)
- Distribution of the values is known in healthy people:

Normal distribution (often)


Sometimes lognormal distribution, "Galton's distribution"


## Examples of distribution in healthy people

## Normal distributions:

Hemoglobinemia in g/dl


Platelet rate in $109 /$


## Lognormal distributions:

TSH plasmatic concentration in $\mathrm{mUI} / \mathrm{l}$


Ferritin plasmatic concentration in $\mathrm{ng} / \mathrm{ml}$


## How is the normality range defined?

- The normality range is defined by the interval containing $95 \%$ of the values of healthy people
- Normal distribution: [ $\mu$-2ds ; $\mu+2 d s$ ]
- Comparable for lognormal distribution
- Other distributions: defined by the quantiles [ $\mathrm{F}^{-1}(0.025) ; \mathrm{F}^{-1}(0.975)$ ]
- Immediate consequence: $5 \%$ of healthy people have "abnormal" values!!
- In the next slides, we will assume that only one of the thresholds is used, to simplify things.


## Usage of a biological parameter to detect ill people

Distribution of parameter in healthy people and ill people.


## Alpha and beta risks of a diagnostic test

- Alpha risk (type 1 error): declaring that a patient is ill despite he is healthy = 1 -Sp
- Beta risk (type 2 error): declaring that a patient is healthy despite he is ill $=1-\mathrm{Se}$
- Power $=1-\beta=$ Se : probability that a ill patient is declared ill


## Unknown realty



## Alpha risk, beta risk, power

Distribution of parameter in healthy people and ill people. Representation of the chosen threshold.

Zone of the Alpha risk


Zone of the beta risk


Beware, in this example ill people have higher values than healthy people.

Alpha risk (probability)


Beta risk (probability)


Power (probability)


Probability that healthy people are declared ill $=1-S p$

Probability that ill people are declared healthy $=1$-Se

Probability that ill patients are declared ill $=S e$

## Consequences of the thresholds on alpha and beta risks



In this example (because ill people have higher values) :
Increase of the threshold =>

- Decrease of alpha risk
- Increase of beta risk
- Decrease of power

Decrease of the threshold =>

- Increase of alpha risk
- Decrease of beta risk
- Increase of power


## Some distributions of biological parameters may vary depending on the subpopulation

- Example: red cells blood concentration (en $10^{6} / \mathrm{\mu l}$ )
- Variation of normal values among 3 populations
- The range used for diagnosis have to be adapted

| Population | Lower <br> bound | Upper <br> bound |
| :--- | :---: | :---: |
| Male adult | 4.5 | 6.2 |
| Female adult | 4 | 5.4 |
| Newborn | 5 | 6 |



## Some distributions of biological parameters may vary depending on the subpopulation

- For example, if we use the boundaries of adult males for adult females, we obtain:
- For too high values detection: beta risk $\uparrow$, alpha risk $\downarrow$
- For too low values detection: alpha risk $\uparrow$, beta risk $\downarrow$

| Population | Lower <br> bound | Upper <br> bound |
| :--- | :---: | :---: |
| Male adult | 4.5 | 6.2 |
| Female adult |  |  |

- For some parameters, the boundaries are adapted depending on the subpopulation
 the patient belongs to.


## Effect of multiple testing in healthy people

- With 1 test:
- probability that healthy people are declared ill = alpha risk = 5\%
- Scenario with several tests:
- k independent laboratory tests are realized
- The patient is declared ill if at least one of the $k$ tests is positive (for each test, $\alpha_{\text {indiv }}=5 \%$ )
- If the patient is healthy, what is the probability to declare him ill?
- $\alpha_{\text {total }}=1-\left(1-\alpha_{\text {indiv }}\right)^{k}$
- => inflation of the $\alpha$ risk.


## Effect of multiple testing in healthy people

## - => inflation of the $\alpha$ risk.



